

Letter to ESEX

Determining hydraulic resistance in gravel-bed rivers from the dynamics of their water surfaces

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Abstract

Traditionally, approaches to account for the effect of the boundary roughness of a gravel-bed river have used a grain-size index of the bed surface as a surrogate for hydraulic resistance. The use of a single grain-size does not take into account the spatial heterogeneity in the bed surface and how this heterogeneity imparts resistance on the flow, nor the way in which this relationship changes with variables such as flow stage. A new technique to remotely quantify hydraulic resistance is proposed. It is based on measuring the dynamics of a river's water surface and relating this to the actual hydraulic resistance created by a rough sediment boundary. The water surface dynamics are measured using a new acoustic technique, grazing angle sound propagation (GRASP). This proposed method to measure hydraulic resistance is based on a greater degree of physical reasoning, and this is discussed in the letter. By measuring acoustically the temporal dynamics of turbulent water surfaces over a water-worked gravel bed in a laboratory flume, a dependency is demonstrated between the temporal variation in the reflected acoustic pressure and measured hydraulic resistance. It is shown that the standard deviation in acoustic pressure decreases with increasing hydraulic resistance. This is shown to apply for a range of relative submergences and bed slopes that are typical of gravel-bed rivers. This remote sensing technique is both rapid and inexpensive, and has the potential to be applied to natural river channels and to other environmental turbulent flows, such as overland flows. A whole new class of low-cost, remote and non-intrusive instruments could be developed as a result and used in a wide range of hydraulic and hydrological applications. Copyright © 2006 John Wiley & Sons, Ltd.

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Introduction

A key problem in fluvial geomorphology has been the evaluation of the resistance imposed by different bed morphologies on the flow (Rouse and Ince, 1963). The determination of this flow resistance is a fundamental requirement for the prediction of flow depth, and thus the calculation of channel flood capacity and bed shear stress to estimate sediment entrainment and transport. Yet the ways in which this resistance is determined still remain crude. The magnitude of the resistance is known to be a function of the geometry of the bed surface. This geometry can only be fully characterized by considering the grain-size distribution, grain shape, grain orientation, bed arrangement, and concentration and geometry of features on the bed surface (Robert, 1990). Generally, in rivers, boundary roughness has been determined by accounting for the effects of all these features with a single coefficient k_s , the equivalent sand roughness height, such that for uniform, steady flow the mean velocity at a given cross-section \bar{U} is estimated by (Keulegan, 1938)

$$\bar{U} = \sqrt{gdS} [6.25 + 5.75 \log(d/k_s)] \quad (1)$$

where g is the acceleration due to gravity, d is the water depth and S is the channel slope. Traditionally, a particle diameter at a certain percentile of the grain-size distribution of the bed material has been used to define k_s . In general, this has been set equal to the order of $3.5D_{84}$ or $6.8D_{50}$ (see, e.g., Hey, 1979; Bray, 1982). This approach assumes that the effect of the bed on the flow is spatially constant and has the same effect at all sites and at all flows, but in reality river bed surfaces are highly irregular and their effects are known to be greater at low flows than at high flows (Griffiths, 1989). As such, the hydraulic roughness characteristics of a river bed are poorly described and are poorly approximated by the use of a single grain-size index, for which the underlying physical basis is unclear. It is clear that alternative approaches to determining hydraulic resistance, which adopt a greater degree of physical reasoning, are required.

Several studies of flow turbulence have shown that the generation and evolution of vortically based large-scale flow structures create quasi-cyclic but persistent flow patterns over water-worked gravel beds (Kirkbride and Ferguson, 1995; Ferguson *et al.*, 1996; Dinehart, 1999; Buffin-Bélanger *et al.*, 2000; Shvidchenko and Pender, 2001; Roy *et al.*, 2004). Once these features are formed, they migrate downstream, deform and amalgamate and produce circular regions of local upwelling on the water surface. Jackson (1976) was the first to describe a scenario in which a vortical flow structure interacts with the water surface, creating secondary vortices. Some studies have suggested that boil generation is the result of flow separation behind dunes. But, other studies have found that surface upwellings occur without the presence of significant bedforms (Kumar *et al.*, 1998), and others have argued that there may be several different generation mechanisms for such water surface features (Kostaschuck and Church, 1993; Babakaiff and Hickin, 1996). Observations and measurements of vertical distributions of turbulent flow properties have indicated that large-scale flow structures dominate the transfer of fluid momentum and hence frictional losses between the bed and the fluid (Robert *et al.*, 1996; Buffin-Bélanger *et al.*, 2000). It appears reasonable, therefore, that an examination of the temporal dynamics of a water surface, and the expression of the large-scale flow structures beneath, may provide potential information about the resistance exerted by a water-worked sediment bed on the flow. This type of observation would be able to take into account the spatial roughness characteristics of the bed surface through the physical effect this has on the flow, something which is not described by the use of a grain-size index. Such an approach demonstrates a stronger degree of physical reasoning and, to the best of our knowledge, has not been carried out before.

It has been long realized that forward- or back-scattering strength and statistics of a transmitted signal can be linked to the spatial spectrum of a dynamically rough interface. In this context, sonar and radar methods have been previously developed for the characterization of the scattering strength of the fluid–air interface (Jackson *et al.*, 1992; Dahl, 1999). These have been primarily used to study long-range underwater sound propagation and echo-sounding in open seas. Empirical spectra have been proposed (Kitaigorodskii, 1983; Durden and Vesecky, 1985) and used to relate wind speed to the spectral density of the sea surface roughness. This has been achieved successfully for the characterization of the dynamic ocean interface by relating the empirical spectra to the acoustic/electromagnetic scattering cross-section.

This paper attempts to develop an existing technique within acoustic engineering to remotely determine the hydraulic resistance imposed by water-worked gravel beds. The temporal dynamics of water surfaces over these beds are measured acoustically, for a range of flows simulated in a laboratory flume for which the hydraulic resistance has been quantified. The data presented shows that a relationship exists between hydraulic resistance and water surface behaviour. The potential application of this method for remote physical measurement of this resistance is also discussed.

Methodology

Grazing angle sound propagation

Recent advances in the study of the acoustics of rough surfaces have revealed that grazing angle sound propagation (here termed GRASP) can be used to determine remotely the geometrical and statistical characteristics of rough solid surfaces (Attenborough and Taherzadeh, 1995; Chambers and Sabatier, 2002) and fluid surfaces (Dahl, 1999). These studies have shown that GRASP has the potential to measure the typical scales of topographical variation in water surfaces for turbulent flows over rough sediment beds. This acoustic approach is based on the assumption that the surface roughness causes a certain perturbation to the acoustic wave R emitted by a point source, and that the reflections by the rough boundary Γ are received at a point receiver (Figure 1). The total sound pressure field at the receiver is $p = g_0 + p_\beta$, where

$$g_0 = -\frac{e^{-ikR}}{4\pi R} - \frac{e^{-ikR_i}}{4\pi R_i} \quad (2)$$

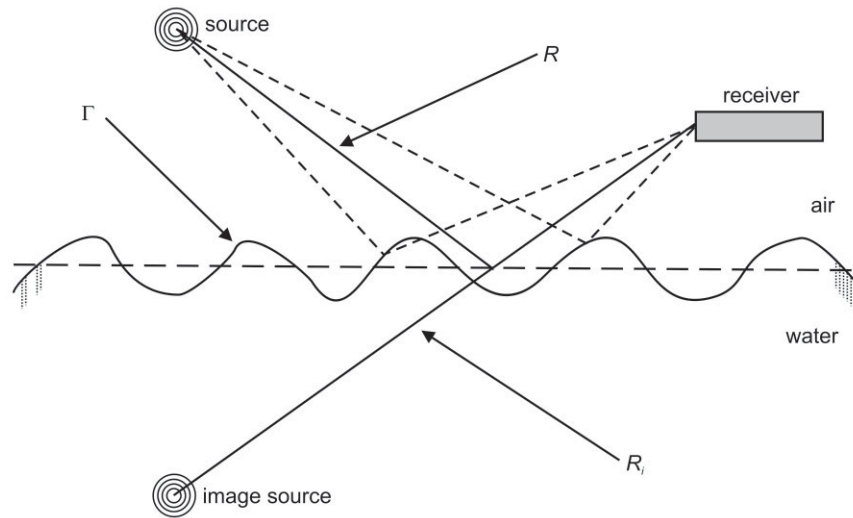


Figure 1. Schematic representation of the acoustic detection of dynamic roughness, whereby the surface roughness (in this case the water surface) Γ causes a perturbation in an acoustic wave R emitted by a point source, and reflections from the boundary are received at a point receiver.

is the Green's function for sound propagation over a plane rigid boundary and

$$p_\beta = \frac{ik\beta}{4\pi} \int_{-\infty}^{\infty} \frac{e^{i(z+z_s)\sqrt{k^2-s^2}} H_0^{(1)}(sr)s}{\sqrt{k^2-s^2}(\sqrt{k^2-s^2}+k\beta)} ds \quad (3)$$

is the perturbation term due to the surface roughness. In these expressions r is the horizontal distance between the source and receiver, k is the acoustic wavenumber, z and z_s are the receiver and source heights, respectively, $H_0^{(1)}(x)$ is the Hankel function of the first kind of zero order of some quantity x and parameter β is the acoustic surface admittance. In the case of a perfectly smooth, rigid boundary the value of the admittance is $\beta = 0$ and the sound pressure is $p \equiv g_0$. It was shown by Attenborough and Taherzadeh (1995) that in the case of an acoustically rigid boundary composed of stationary hemispheres of radius a (analogous to water surface upwellings) the acoustic admittance is purely imaginary and given by

$$\beta = -ik \frac{\pi^2 N a^3}{3} \left(1 - \frac{\pi^2 a^3}{4l^3} \right) \left(1 + \frac{\pi^2 a^3}{4l^3} \right) \quad (4)$$

where $i = \sqrt{-1}$, N is the average density of hemispheres per unit area and $l \approx \sqrt{N}$ is the mean spacing between the hemispheres. Equations (2)–(4) suggest that the acoustic pressure at the position of the receiver should depend on the instantaneous radius of the hemispheres and their spatial distribution. Applying the Thomasson (1980) approximation for integrals to Expression (3), we find that for grazing angles of sound propagation the acoustic pressure perturbation is $p_\beta \sim \beta e^{ikr}/r$, which incorporates the effect of the surface roughness. We note that this effect is averaged over the intersection of the Fresnel ellipsoid and the reflecting boundary (Hothersall and Harriott, 1995). Here, the Fresnel ellipsoid can be defined as an ellipsoid with the minor axis of radius $\lambda/3$ and the foci being at the image source point and the acoustic receiver, where λ is the acoustic wavelength.

The above approach was exploited to examine the temporal dynamics of water surfaces under varying hydraulic conditions in order to determine whether hydraulic resistance can be related directly to acoustic measurements of a dynamic water surface. It involved the use of a tweeter and microphone which were set 60 mm and 40 mm above the average level of the water surface, respectively, and placed on the centreline of the flume (Figure 2). The tweeter generated linear, sinusoidal sweep acoustic pressure signals of 20 ms duration in the frequency range of 1–40 kHz,

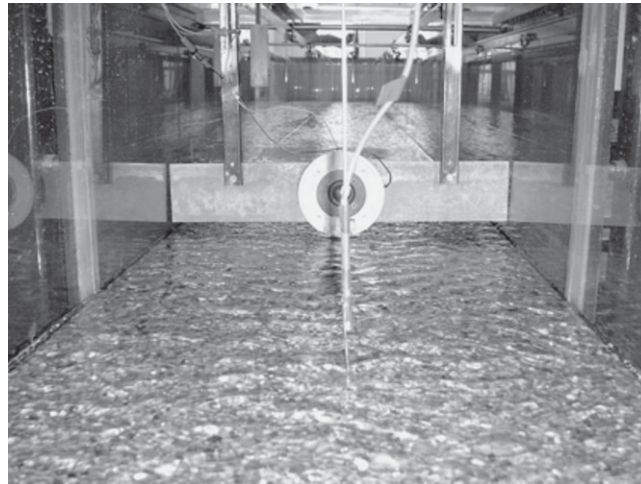


Figure 2. The experimental arrangement of the acoustic equipment, showing the microphone mounted on a thin rod from the flume rails in the foreground and the circular tweeter mounted on a horizontal traverse in the background. As a guide for scale, the separation between the glass walls of the flume is 0.5 m.

which were produced periodically at 100 ms intervals. A total of 40 sweeps were deployed for each water surface investigated. The signal was reflected by the water surface and the glass-sided walls of the flume. These signals were recorded by a 1/4" microphone and de-convolved to determine the acoustic impulse response of these features. An Adrienne time window of 0–1.4 ms was employed to control the multiple reflections from the glass walls so that the reflections from the water surface were optimized (Figure 3). A distance of 0.5 m was used between the microphone and the tweeter. This separation was found to allow the full development of the interference pattern between the outgoing acoustic wave and the acoustic wave reflected by the water surface. This in turn controlled the reflections received from the flume walls. The tweeter emitted a spherical wave so the water surface was acoustically detected over a streamwise distance of 0.5 m. The width of the detected area of which the reflections from the water surface were of importance was approximately equal to $\lambda/3$. Given that the tweeter was operated at a minimum frequency of 1 kHz, this resulted in a maximum width of 0.1 m. This experimental set-up produced a signal-to-noise ratio of greater than 20 dB in the frequency range of 2–30 kHz. The acoustic impulse response from the water surface for each of the 40 sweeps was determined by separating the acoustic pressure response received at the microphone from the radiated sinusoidal sweep stimulus. The standard deviation at time t of the 40 responses $\sigma_p(t)$ was considered to be an appropriate measure of the temporal variation in the elevation of the water surface and was given by

$$\sigma_p(t) = \sqrt{\frac{\sum_{j=1}^{40} (p_j(t) - \bar{P}(t))^2}{40}} \quad (5)$$

where $p_j(t)$ is the acoustic pressure response for response j at t , and $\bar{P}(t)$ is the acoustic pressure response averaged over 40 responses at t .

Experimental set-up

The tests were conducted in an 18 m long, 0.5 m wide laboratory flume, which could be tilted to produce a range of channel slopes. Consideration was made of how to produce a bed representative of a natural river, so that a realistic scale of boundary roughness was produced. Many previous laboratory studies have placed a sediment into the base of a flume and scraped it flat to a particular bed depth. Measurements are then made either over this bed, or after the bed has been water-worked for a period of time. Visually, this method appears to result in the sediment deposit having a lower degree of particle imbrication and higher porosity than observed in natural gravel-bed rivers. The flow fields over such beds may therefore not be fair representations of natural conditions.

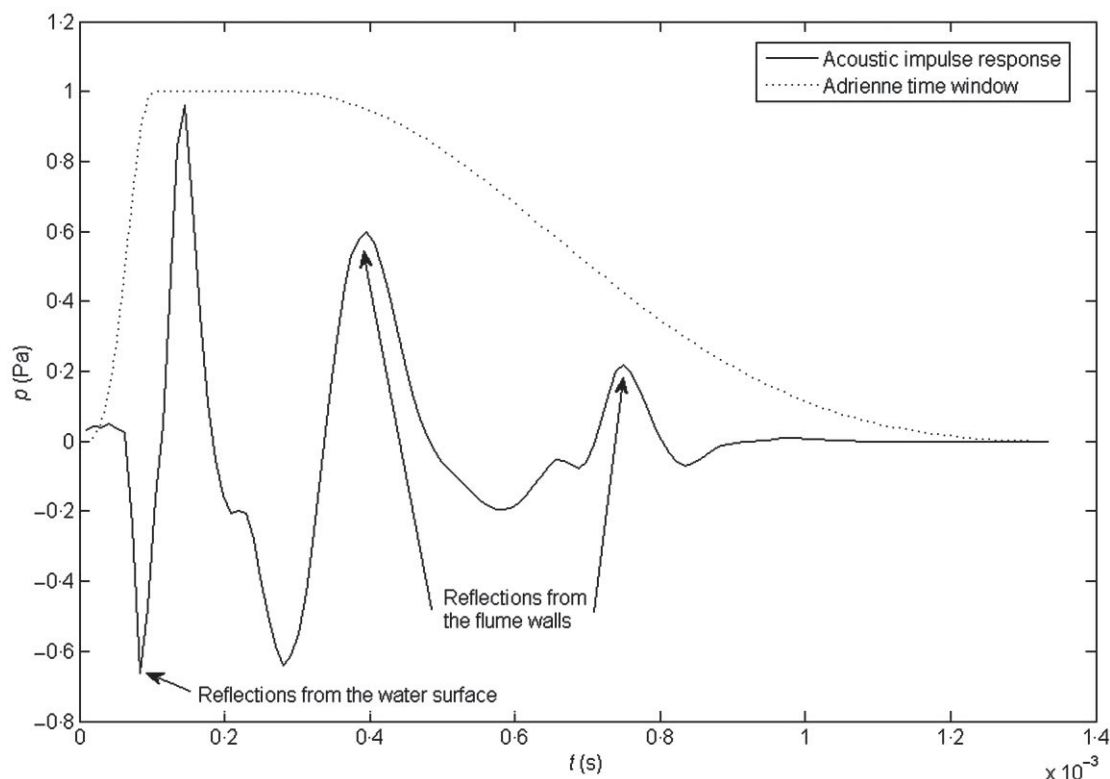


Figure 3. The acoustic pressure response p over time t showing the reflections of one acoustic signal from the water surface and the glass-sided flume walls. Also depicted is the form of the Adrienne time window applied to the acoustic pressure response to control the reflections from the flume walls.

Recently, Barison *et al.* (2003) discovered that the spatial distribution of time-averaged streamwise velocity over sediment beds in the near-bed region was significantly different over flat, scraped beds than over a water-worked bed. Initially when the bed was flat, the distributions were highly positively skewed, with a low proportion of smaller velocities. As the bed surface became more water-worked the distributions became flatter, wider and less skewed. This indicated that the way in which the beds are formed in the laboratory might have an important effect on the flow field.

A different approach to bed production was therefore adopted here. A widely graded river sediment was fed into the flume during conditions in which the bedload transport capacity of the flow, as estimated by Meyer-Peter and Müller (1948), was half of the imposed sediment feed rate. This resulted in the progressive formation of a sloping water-worked gravel bed in the base of the flume (Figure 4(a)). The bed was formed through the movement and rearrangement of the individual grains by the flow, allowing the flow to sort the grains over the flume length. The sediment was fed into the flow with the use of a conveyor belt in order to maintain a steady feed rate. Feeding was halted once a steady bed slope was formed. The sediment mixture had a unimodal and lognormal grain-size distribution encompassing medium sized gravels to fine sands, typical of gravel-bed rivers, with D_{50} of 4.97 mm and D_{84} of 7.00 mm (Figure 4(b)).

A total of 15 hydraulic conditions were investigated (Table I). A range of flow depths was produced so that the ratio of d to D_{84} varied from 2.8 to 12.8, which is believed to be the typical range found in gravel-bed rivers (Robert, 2003). The Reynolds numbers for all flows were high enough to ensure that all flows were fully turbulent. During the testing programme, the slope of the flume was less than that used during the formation of the bed, so that the deposit grains were stationary during all experimental runs. In each run the flume was set at a known channel slope and uniform, steady flow conditions were achieved, after which the water depth was measured and the mean flow velocity was calculated from the ratio of flow discharge to the cross-sectional area of the flow. This data enabled the hydraulic resistance k_s for each flow condition to be calculated using an equation originally developed by Colebrook (1938) for pipes and subsequently extended to open channel flows

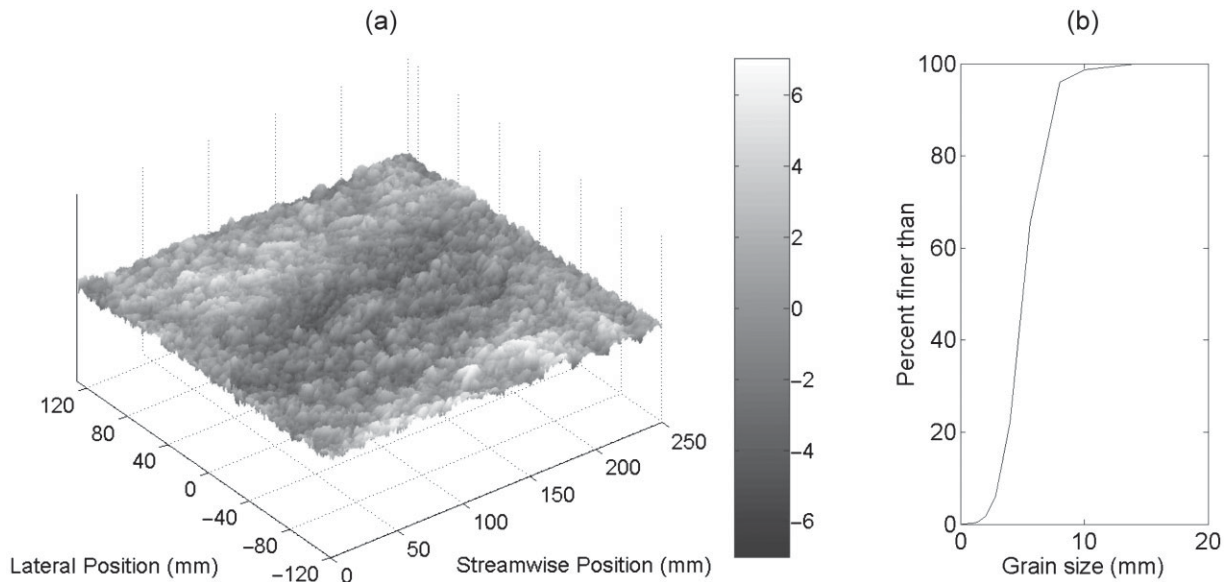


Figure 4. (a) A DEM of a section of the bed over which GRASP measurements were made. This was obtained using a laser displacement sensor measuring at 1 mm intervals in both the streamwise and lateral direction. The grayscale relates to bed surface elevation (mm). A lateral position of 0 mm denotes the centreline of the flume and the increasing values in the streamwise position are in the direction of the flow; (b) grain-size distribution of the sediment mixture used to produce the bed.

Table I. A summary of the investigated hydraulic conditions, where S is the channel slope, d is the water depth, D_{84} is the size of the intermediate axis of the bed grains for which 84 per cent of the bed material is finer, \bar{U} is the average flow velocity (calculated from the ratio of flow discharge to the cross-sectional area of the flow), and Re is the flow Reynolds number (calculated from $\bar{U}d/\nu$, where ν is the kinematic viscosity). It was ensured that a water temperature of approximately 23 °C was maintained so that the kinematic viscosity of the water was constant throughout all the experiments

Run	S (-)	d (mm)	d/D_{84}	\bar{U} (m/s)	Re (-)	k_s (mm)
1	0.00285	19.4	2.8	0.16	2 328	15.0
2	0.00285	30.6	4.4	0.25	5 773	10.4
3	0.00285	38.9	5.6	0.29	8 727	9.9
4	0.00285	49.2	7.0	0.34	12 925	9.6
5	0.00285	63.7	9.1	0.44	21 108	6.7
6	0.00285	89.7	12.8	0.58	39 669	3.9
7	0.00375	43.2	6.2	0.36	11 811	10.2
8	0.00375	49.4	7.1	0.40	14 928	9.5
9	0.00375	61.0	8.7	0.50	23 281	5.8
10	0.00465	29.5	4.2	0.29	6 477	13.1
11	0.00465	37.9	5.4	0.36	10 491	10.6
12	0.00555	32.8	4.7	0.35	8 763	11.6
13	0.00555	39.7	5.7	0.44	13 149	8.3
14	0.00645	32.7	4.7	0.37	9 298	12.2
15	0.00735	29.1	4.2	0.37	8 188	11.9

$$U = -\sqrt{(32gRS)} \log_{10} \left(\frac{k_s}{14.8R} + \frac{1.225\nu}{R\sqrt{(32gRS)}} \right) \quad (6)$$

where R is the hydraulic radius, defined as the ratio of cross-sectional area of the channel to the wetted perimeter, and ν is the kinematic viscosity. The temporal dynamics of the water surface was then measured using GRASP at a distance of 10 m from the flume inlet.



Figure 5. Still images of two water surfaces. These have been taken for two experimental runs at the same channel slope but with different levels of hydraulic resistance. As a guide for scale, the separation between the glass walls of the flume is 0.5 m. The flow direction is into the page. (a) Experimental run 1, $d = 19.4$ mm, $k_s = 15.0$ mm. The microphone is visible in the centre of the image; (b) Experimental run 6, $d = 89.7$ mm, $k_s = 3.9$ mm.

Results

Visual records were made of the water surfaces for several hydraulic conditions in order to examine whether the dynamics of the water surfaces changed with hydraulic resistance. Two images of water surfaces taken over the measurement area are provided as a visual guide to the range of the water surface behaviour observed (Figure 5). It can be seen that the water surface with a relatively high level of hydraulic resistance and a low water depth (Figure 5(a)) is characterized by many small upwellings, all of which are elongated laterally. In contrast, the surface with a low level of resistance and deeper water (Figure 5(b)) is much rougher in appearance and dominated by a smaller number of much larger upwellings, resembling a train of standing waves, as found in critical flow (Tinkler, 1997). Surrounded by these upwellings is a much flatter water surface.

An examination of the change in $\sigma_p(t)$ with k_s provides a quantitative measure of the relationship between the temporal dynamics of the water surface and hydraulic resistance (Figure 6). The results presented in Figure 6 were obtained by averaging the standard deviation in the acoustic impulse response within the time window shown in Figure 3. For clarity, only runs 1, 2, 3 and 6 have been included in Figure 6 along with the data from a still water surface as a basis for comparison. This shows that the standard deviation generally decreases for flows with higher k_s values. This effect is particularly pronounced for the peak values in the time period of 0.135–0.156 ms. This time interval corresponds to the time of the arrival of the first acoustic reflections from the water surface. Outside this time period the effect of the roughness of the water surface on the acoustic impulse response is limited and the acoustic signal is contaminated with reflections from the walls of the flume (see Figure 3).

It is this time interval of 0.135–0.156 ms that appears to be of most interest in determining whether the acoustic reflections from the water surface can determine hydraulic resistance. By examining the standard deviation in the acoustic pressure response averaged over this time interval $\langle \sigma_p^2 \rangle$ and how this varies with k_s , the potential of this application can be discovered (Figure 7). It is clear that there is a dependence between $\langle \sigma_p^2 \rangle$ and k_s . The temporal variation in the acoustic pressure reduces with increasing k_s values.

Discussion and Potential Applications

This work demonstrates that the temporal dynamics of a water surface, reflected in the temporal deviation of its acoustic response, has the potential to be used for determining hydraulic resistance in gravel-bed rivers. A wide range of hydraulic conditions was explored, representing a realistic range of relative submergences and channel slopes. This, combined with the high Reynolds numbers, indicates that the results would scale to the range of hydraulic conditions found in gravel-bed rivers. GRASP offers the potential for estimating hydraulic resistance at different river stages,

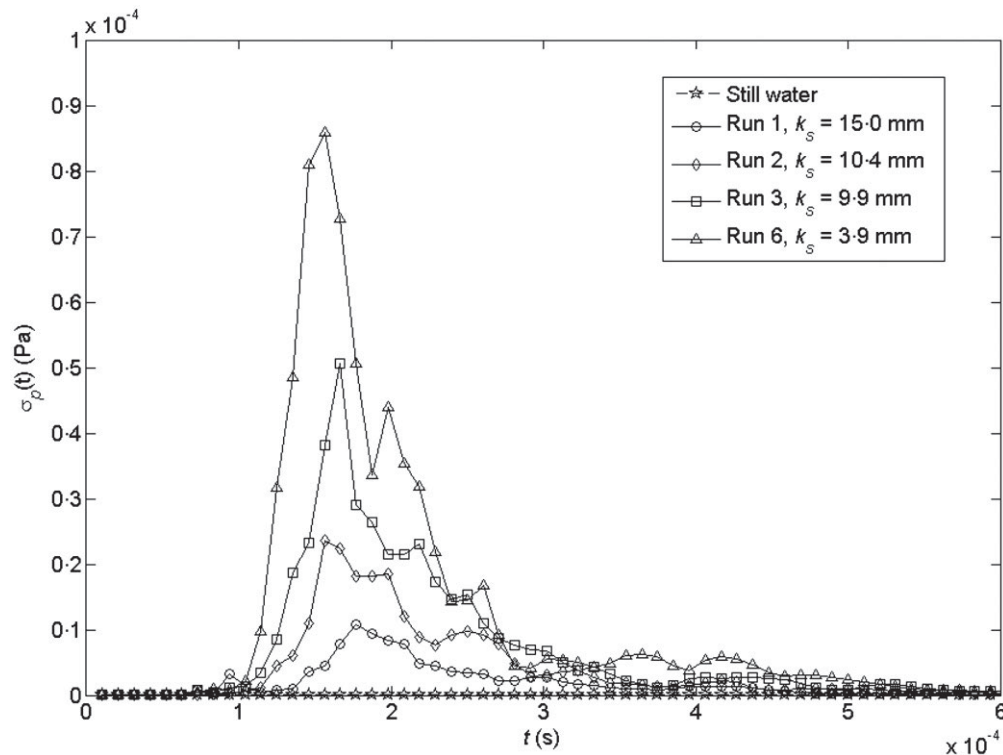


Figure 6. The change in the standard deviation in the acoustic impulse response $\sigma_p(t)$ with time t . Four hydraulic conditions are shown in order to show how the acoustic response changes with hydraulic resistance, and these are compared with a still water surface.

unlike through the use of a single grain-size index, in which the choice of grain-size involves no consideration of the variations in water depth or bedform geometries. This means that rapid measurement of hydraulic resistance could be achieved, which would allow the assessment of temporal changes in resistance during floods. This newly developed technique could also be used for a given river at different locations along its downstream course. Also, it does not require the time-consuming task of measuring the grain-size distribution of a river bed, which without careful sampling design can poorly represent the actual grain size-distribution and cause uncertainties in the estimates of boundary roughness.

The acoustic technique presented here determines hydraulic resistance by considering the interaction between the bed surface and the internal flow structure, and then examining the manner in which the internal flow structure is reflected in the dynamics of the water surface. As such, this technique has a strong element of physical reasoning, and its use in different river environments is not likely to be restricted by assumptions and simplifications that are inherent in the application of the grain-size index method. It therefore has the potential to be more widely applied to rivers with different morphologies and for the study of other turbulent flows, such as overland and in-pipe flows. The physical basis of GRASP means that it can provide estimations of boundary roughness that are responsive to changes in water depth. This technique is non-intrusive, inexpensive and rapid and is able to predict hydraulic resistance at times when this data is needed quickly, such as in flood forecasting. It will open up significant possibilities for river managers; model calibration could be significantly improved and on-line real-time monitoring become a realistic option.

Work has already begun on investigating the relationship between large-scale flow structures and momentum exchange between the fluid and the bed, and the effects of relative submergence on the expression of these flow structures at the surface (and therefore on hydraulic resistance). Detailed 2D particle image velocimetry (PIV) measurements in a plane normal to the bed surface have been made at several lateral locations over the bed for 12 of the flows investigated in this letter. Conductivity wave-probes have been used to measure the temporal changes in the water surface elevation, with the view that the power spectrum of the variations can be compared to that of the acoustic and velocity measurements. Further application of GRASP is required for gravel beds of different surface topographies in order to understand fully the potential of this approach for determining hydraulic resistance in gravel-bed rivers. Consideration is required to the calibration and scaling up of the proposed technique for field measurement.

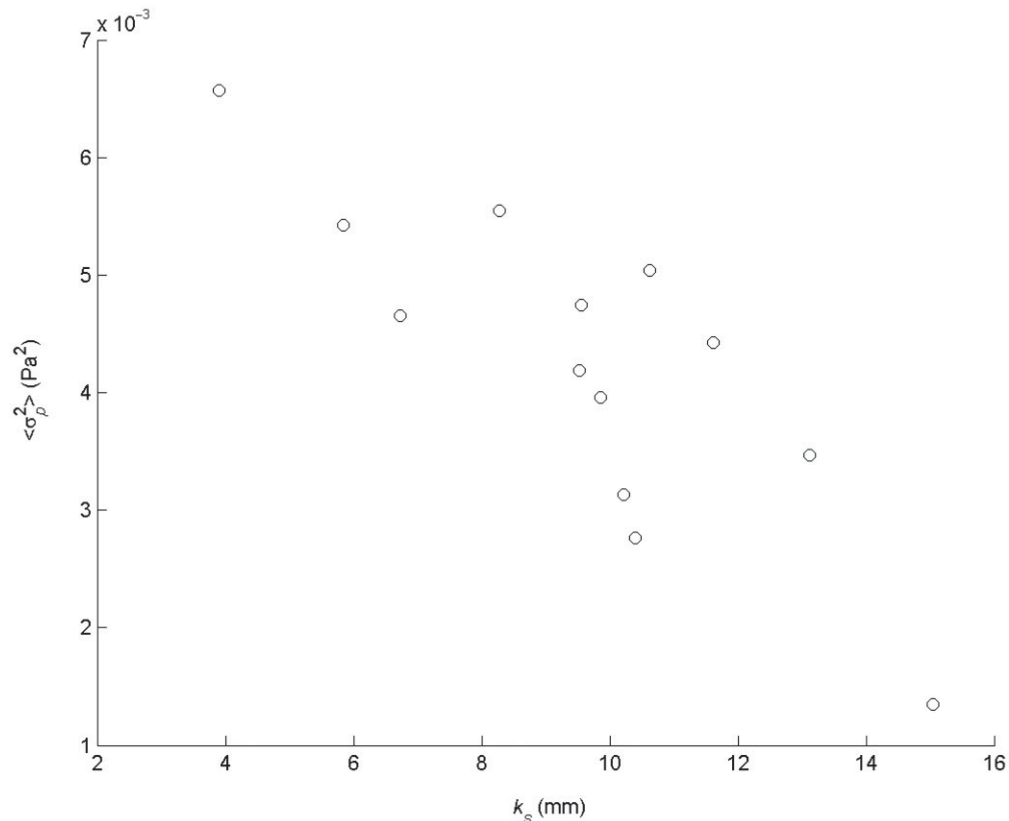


Figure 7. The standard deviation in acoustic impulse response averaged over the time interval $0.135 \leq t \leq 0.156$ ms $\langle \sigma_p^2 \rangle$ against hydraulic resistance k_s . This time interval corresponds with the time of the arrival of the first acoustic reflections from the water surface within each acoustic response. All fifteen experimental runs outlined in Table I are displayed.

Equation (4) suggests that the transition from a small laboratory to a large-scale *in situ* environment may require a proportional decrease in the frequency of the emitted sound in order to be able to remotely sense larger-scale water surface roughness observed in natural rivers and open channels.

The work reported in this letter aims to promote further studies into the dynamics of turbulent water surfaces, a currently neglected area of study. Although this letter has examined its potential for determining hydraulic resistance, it is clear that the water surface has the potential to provide additional information on the main structural aspects of the flow, and may provide insights into the behaviour of coherent flow structures that may not be easily detectable in velocity data. The data presented in this letter should encourage the development of a whole new class of instrument: remote, non-intrusive, low cost and deployable in a wide range of fluvial environments.

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